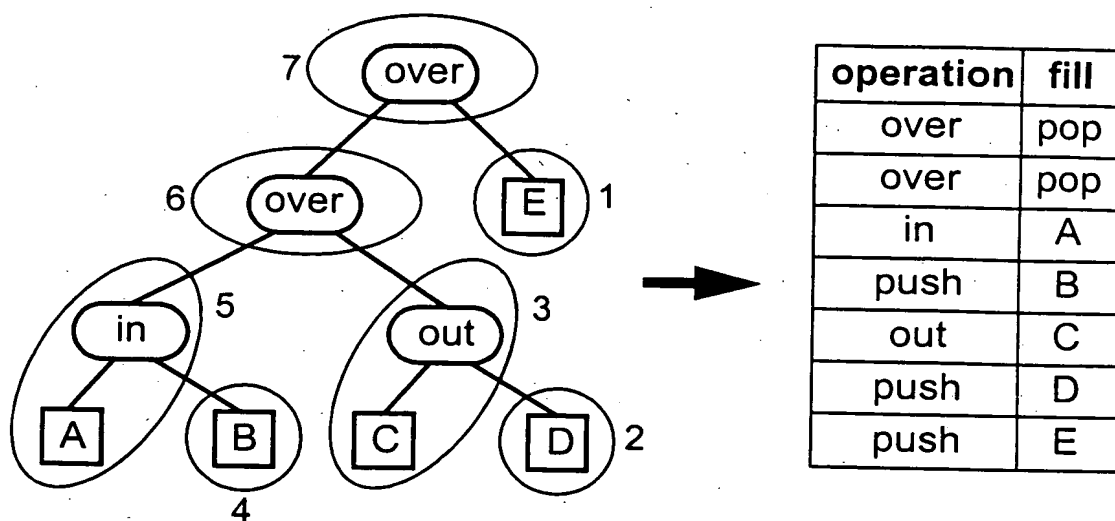
**Fig. 1**



**Fig. 3**

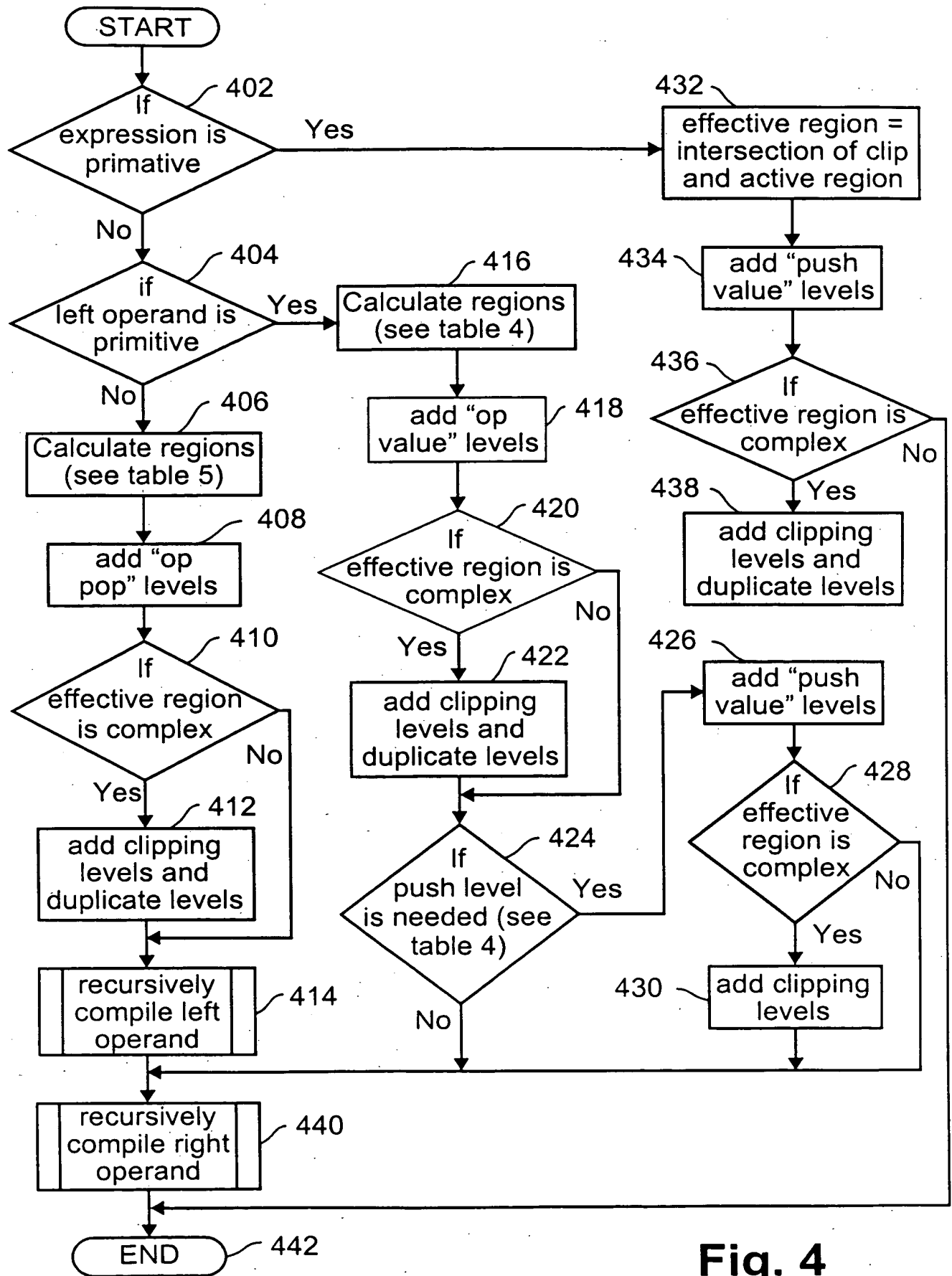


Fig. 4

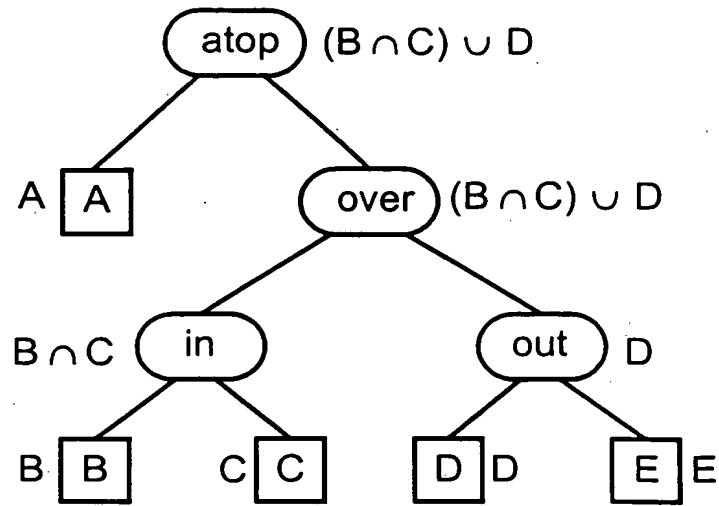


Fig. 5

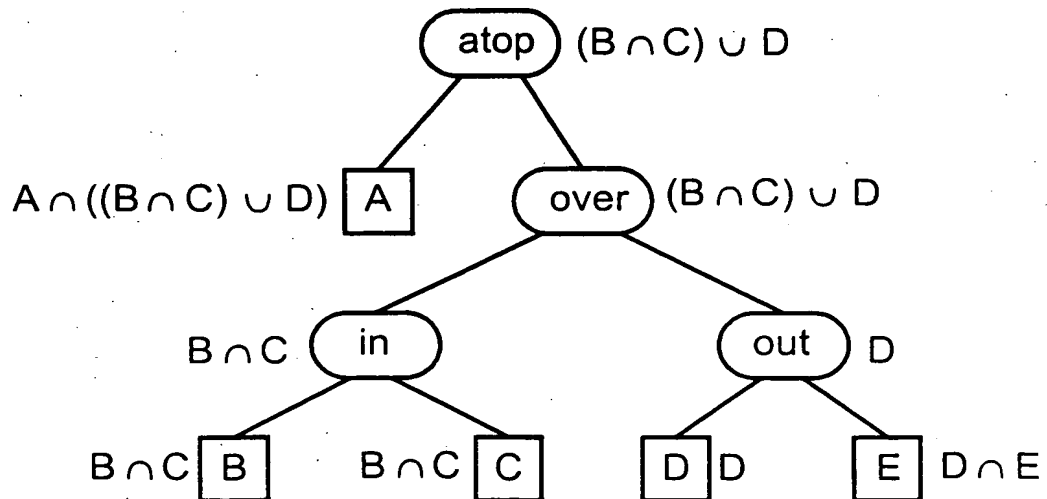
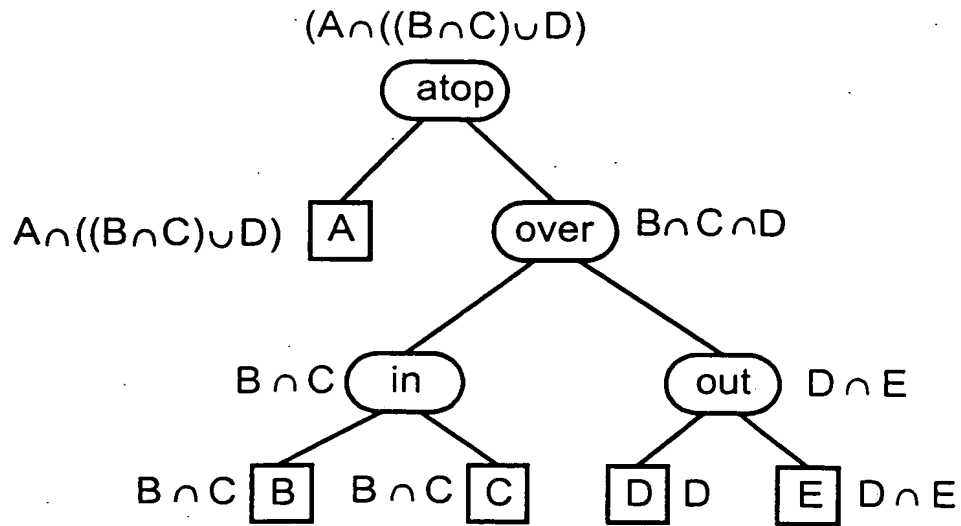
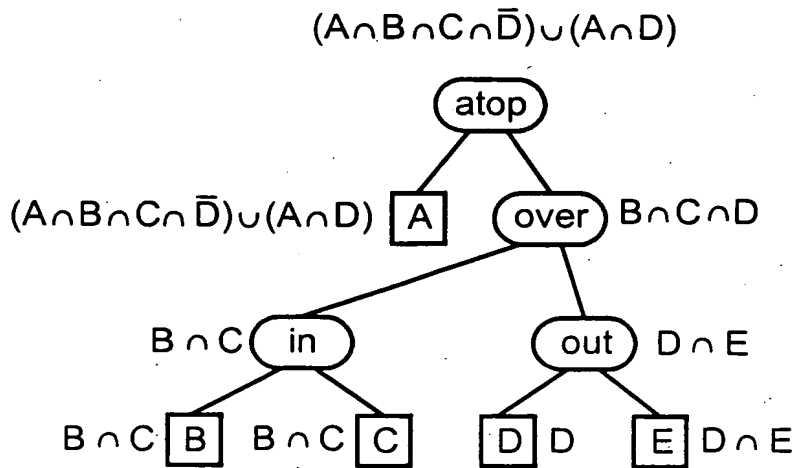


Fig. 6

**Fig. 7**

operation	fill
atop	A
atop	A
over	pop
in	B
push	C
out	D
push	D
push	E
clip	E
clip	\bar{E}
clip	C
clip	B
clip	D
clip	\bar{D}

Fig. 8

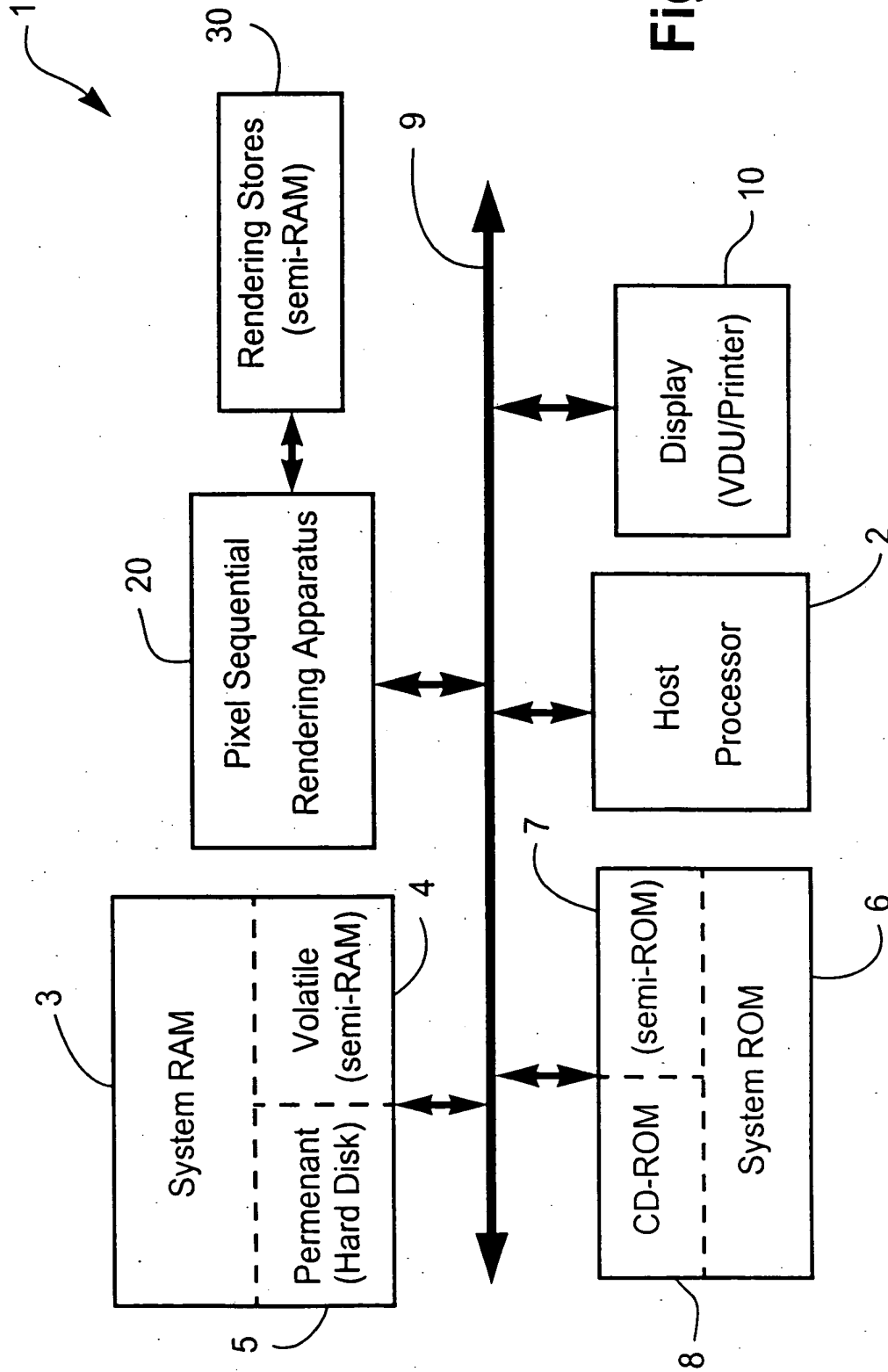
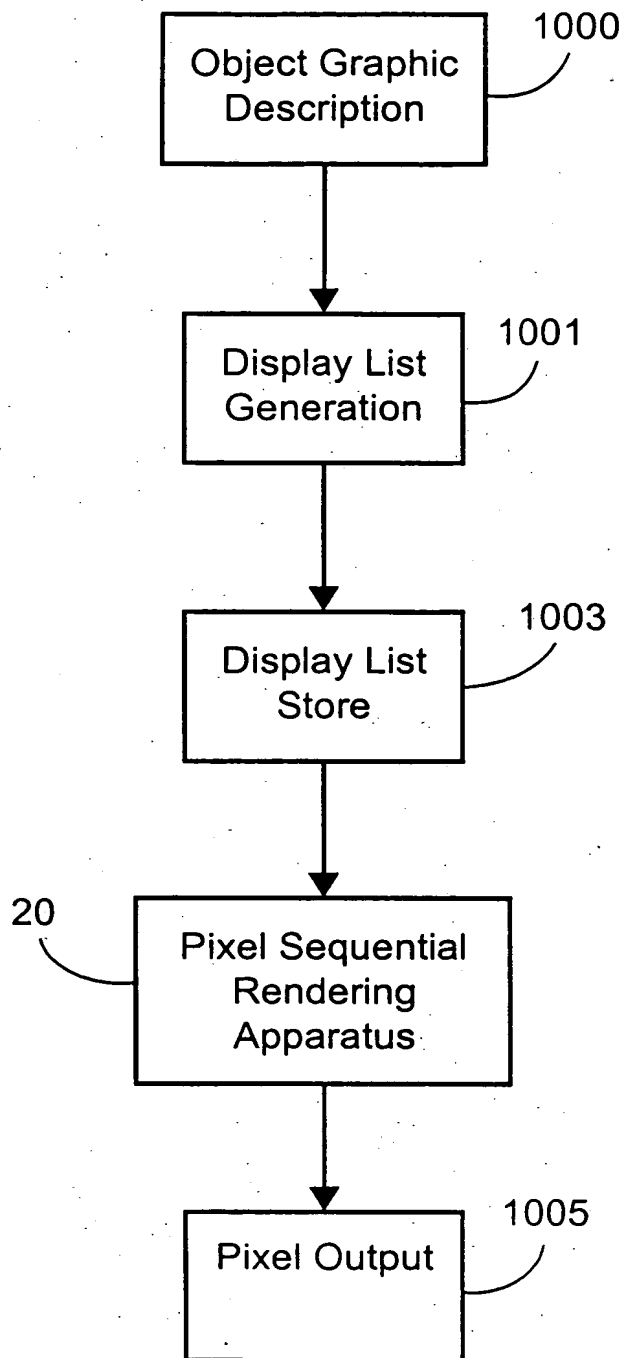
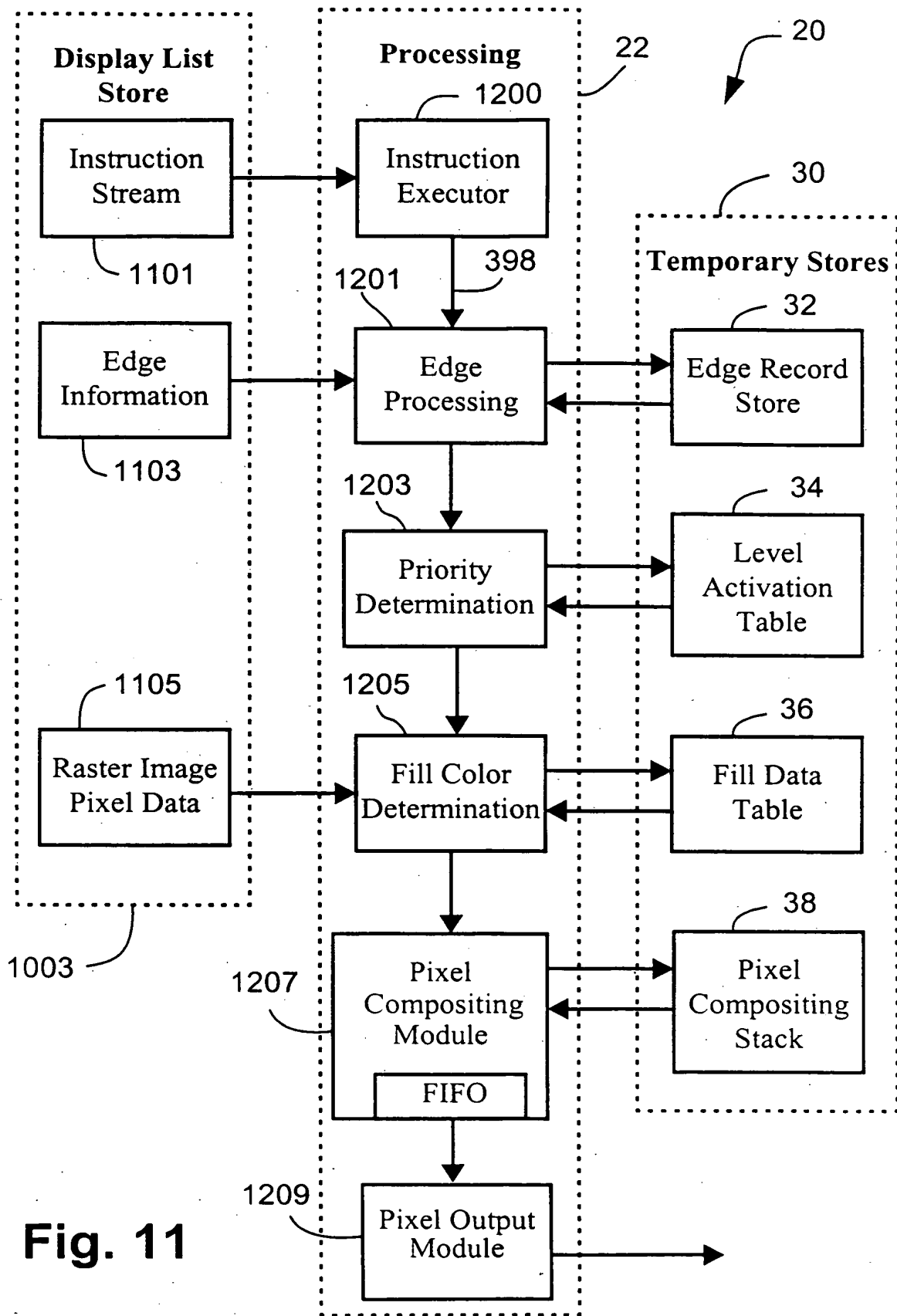
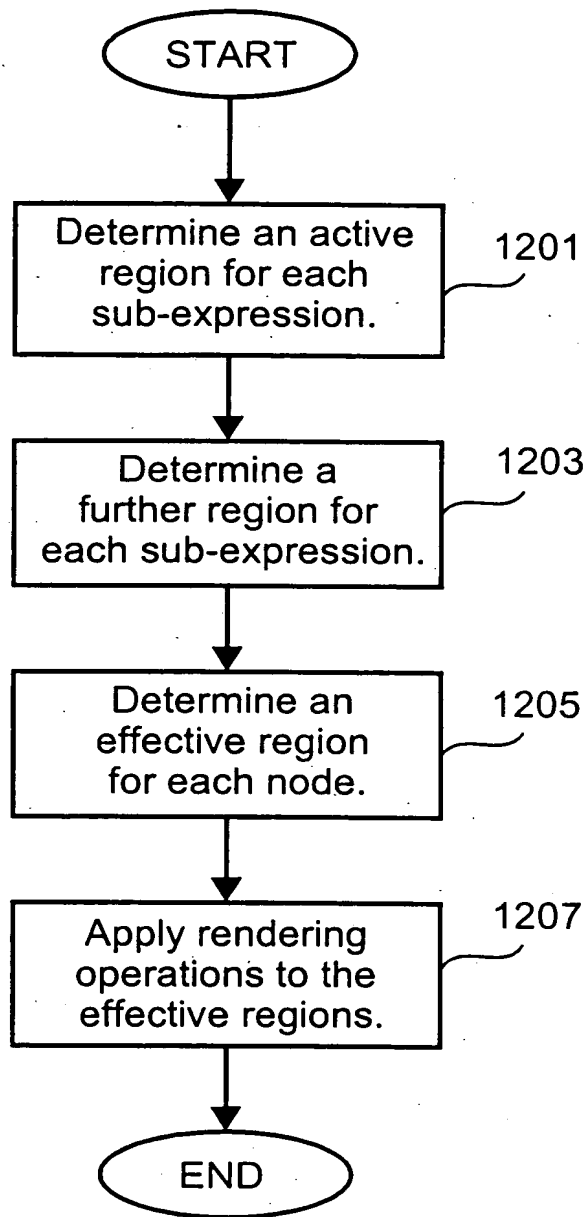
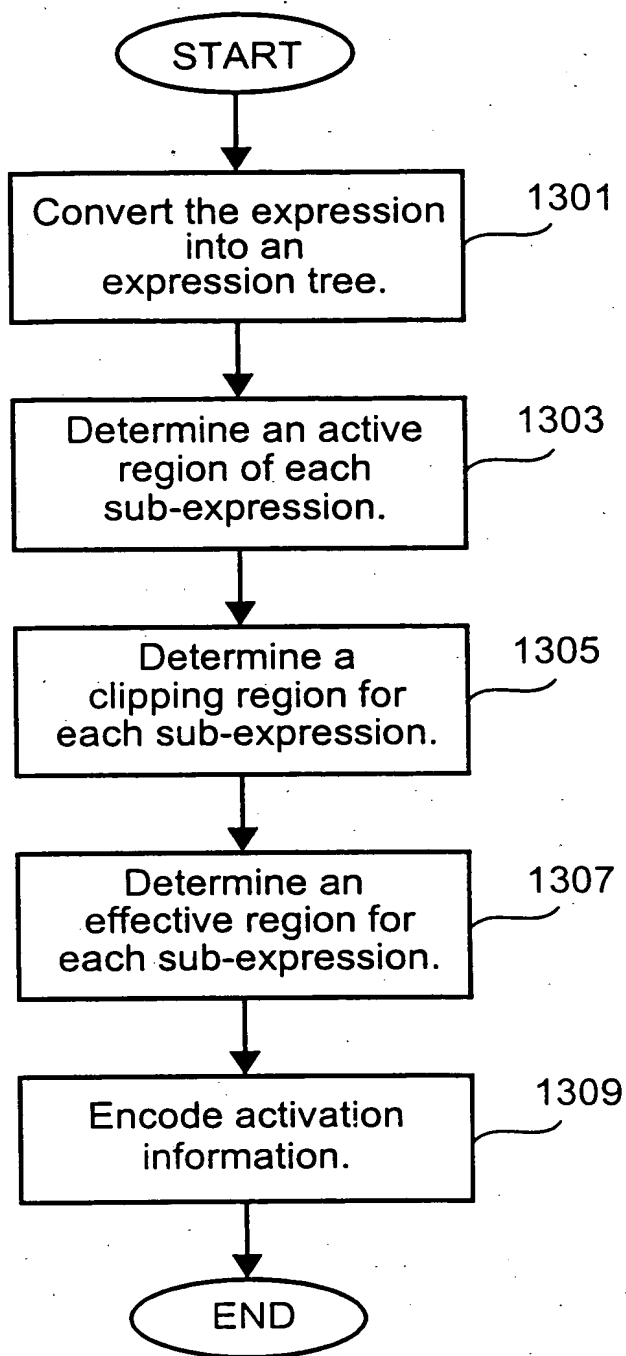


Fig. 9

**FIG. 10**

**Fig. 11**

**Fig. 12**

**Fig. 13**

Operation	Region	Value	Level	Stack	Result	Correct
A over B	$A \cap B$	A over B	over A	B	A over B	A over pop
	$A \cap \bar{B}$	A		?	A over ?	push A
	$\bar{A} \cap B$	B		B	B	no-op
	$\bar{A} \cap \bar{B}$	glass		?	?	no-op
A rover B	$A \cap B$	A rover B	rover A	B	A rover B	A rover pop
	$A \cap \bar{B}$	A		?	A rover ?	push A
	$\bar{A} \cap B$	B		B	B	no-op
	$\bar{A} \cap \bar{B}$	glass		?	?	no-op
A in B	$A \cap B$	A in B	in A	B	A in B	A in pop
	$A \cap \bar{B}$	glass		?	A in ?	no-op
	$\bar{A} \cap B$	glass		B	B	pop
	$\bar{A} \cap \bar{B}$	glass		?	?	no-op
A rin B	$A \cap B$	A rin B	rin A	B	A rin B	A rin pop
	$A \cap \bar{B}$	glass		?	A rin ?	no-op
	$\bar{A} \cap B$	glass		B	B	pop
	$\bar{A} \cap \bar{B}$	glass		?	?	no-op
A out B	$A \cap B$	A out B	out A	B	A out B	A out pop
	$A \cap \bar{B}$	A		?	A out ?	push A
	$\bar{A} \cap B$	glass		B	B	pop
	$\bar{A} \cap \bar{B}$	glass		?	?	no-op
A rout B	$A \cap B$	A rout B	rout A	B	A rout B	A rout pop
	$A \cap \bar{B}$	glass		?	A rout ?	no-op
	$\bar{A} \cap B$	B		B	B	no-op
	$\bar{A} \cap \bar{B}$	glass		?	?	no-op
A atop B	$A \cap B$	A atop B	atop A	B	A atop B	A atop pop
	$A \cap \bar{B}$	glass		?	A atop ?	no-op
	$\bar{A} \cap B$	B		B	B	no-op
	$\bar{A} \cap \bar{B}$	glass		?	?	no-op
A ratop B	$A \cap B$	A ratop B	ratop A	B	A ratop B	A ratop pop
	$A \cap \bar{B}$	A		?	A ratop ?	push A
	$\bar{A} \cap B$	glass		B	B	pop
	$\bar{A} \cap \bar{B}$	glass		?	?	no-op
A xor B	$A \cap B$	A xor B	xor A	B	A xor B	A xor pop
	$A \cap \bar{B}$	A		?	A xor ?	push A
	$\bar{A} \cap B$	B		B	B	no-op
	$\bar{A} \cap \bar{B}$	glass		?	?	no-op

Table 1

Operation	Region	Value	Level	Stack	Result	Correct
A over B	$A \cap B$	A over B	over	A,B	A over B	over
	$A \cap \bar{B}$	A		A,?	A over ?	no-op
	$\bar{A} \cap B$	B		B,?	B over ?	no-op
	$\bar{A} \cap \bar{B}$	glass		?,?	? over ?	no-op
A rover B	$A \cap B$	A rover B	rover	A,B	A rover B	rover
	$A \cap \bar{B}$	A		A,?	A rover ?	no-op
	$\bar{A} \cap B$	B		B,?	B rover ?	no-op
	$\bar{A} \cap \bar{B}$	glass		?,?	? rover ?	no-op
A in B	$A \cap B$	A in B	in	A,B	A in B	in
	$A \cap \bar{B}$	glass		A,?	A in ?	pop
	$\bar{A} \cap B$	glass		B,?	B in ?	pop
	$\bar{A} \cap \bar{B}$	glass		?,?	? in ?	no-op
A rin B	$A \cap B$	A rin B	rin	A,B	A rin B	rin
	$A \cap \bar{B}$	glass		A,?	A rin ?	pop
	$\bar{A} \cap B$	glass		B,?	B rin ?	pop
	$\bar{A} \cap \bar{B}$	glass		?,?	? rin ?	no-op
A out B	$A \cap B$	A out B	out	A,B	A out B	out
	$A \cap \bar{B}$	A		A,?	A out ?	no-op
	$\bar{A} \cap B$	glass		B,?	B out ?	pop
	$\bar{A} \cap \bar{B}$	glass		?,?	? out ?	no-op
A rout B	$A \cap B$	A rout B	rout	A,B	A rout B	rout
	$A \cap \bar{B}$	glass		A,?	A rout ?	pop
	$\bar{A} \cap B$	B		B,?	B rout ?	no-op
	$\bar{A} \cap \bar{B}$	glass		?,?	? rout ?	no-op
A atop B	$A \cap B$	A atop B	atop	A,B	A atop B	atop
	$A \cap \bar{B}$	glass		A,?	A atop ?	pop
	$\bar{A} \cap B$	B		B,?	B atop ?	no-op
	$\bar{A} \cap \bar{B}$	glass		?,?	? atop ?	no-op
A ratop B	$A \cap B$	A ratop B	ratop	A,B	A ratop B	ratop
	$A \cap \bar{B}$	A		A,?	A ratop ?	no-op
	$\bar{A} \cap B$	glass		B,?	B ratop ?	pop
	$\bar{A} \cap \bar{B}$	glass		?,?	? ratop ?	no-op
A xor B	$A \cap B$	A xor B	xor	A,B	A xor B	xor
	$A \cap \bar{B}$	A		A,?	A xor ?	no-op
	$\bar{A} \cap B$	B		B,?	B xor ?	no-op
	$\bar{A} \cap \bar{B}$	glass		?,?	? xor ?	no-op

Table 2

Expression	Active Region
A over B	$A \cup B$
A rover B	$A \cup B$
A in B	$A \cap B$
A rin B	$A \cap B$
A out B	A
A rout B	B
A atop B	B
A ratop B	A
A xor B	$A \cup B$

Table 3

Operation	Levels	Clip
A over B	over A	clip \cap B
	push A	clip \cap \bar{B}
	table B	clip
A rover B	rover A	clip \cap B
	push A	clip \cap \bar{B}
	table B	clip
A in B	in A	clip \cap B
	table B	clip \cap A
A rin B	rin A	clip \cap B
	table B	clip \cap A
A out B	out A	clip \cap B
	push A	clip \cap \bar{B}
	table B	clip \cap A
A rout B	rout A	clip \cap B
	table B	clip
A atop B	atop A	clip \cap B
	table B	clip
A ratop B	ratop A	clip \cap B
	push A	clip \cap \bar{B}
	table B	clip \cap A
A xor B	xor A	clip \cap B
	push A	clip \cap \bar{B}
	table B	clip

Table 4



Operation	Levels	Clip
A over B	over	clip \cap A \cap B
	table A	clip
	table B	clip
A rover B	rover	clip \cap A \cap B
	table A	clip
	table B	clip
A in B	in	clip \cap A \cap B
	table A	clip \cap B
	table B	clip \cap A
A rin B	rin	clip \cap A \cap B
	table A	clip \cap B
	table B	clip \cap A
A out B	out	clip \cap A \cap B
	table A	clip
	table B	clip \cap A
A rout B	rout	clip \cap A \cap B
	table A	clip \cap B
	table B	clip
A atop B	atop	clip \cap A \cap B
	table A	clip \cap B
	table B	clip
A ratop B	ratop	clip \cap A \cap B
	table A	clip
	table B	clip \cap A
A xor B	xor	clip \cap A \cap B
	table A	clip
	table B	clip

Table 5

Expression	Clip A	Clip B	Active Region	Opaque Region
A over B	A	$B \cap \bar{O}_A$	$A \cup B$	$O_A \cup O_B$
A rover B	$A \cap \bar{O}_B$	B	$A \cup B$	$O_A \cup O_B$
A in B	$A \cap B$	$A \cap B \cap \bar{O}_B$	$A \cap B$	$O_A \cap O_B$
A rin B	$A \cap B \cap \bar{O}_A$	$A \cap B$	$A \cap B$	$O_A \cap O_B$
A out B	$A \cap B \cap \bar{O}_B$	$A \cap B$	$A \cap \bar{O}_B$	$\bar{B} \cap O_A$
A rout B	$A \cap B$	$A \cap B \cap \bar{O}_A$	$B \cap \bar{O}_A$	$\bar{A} \cap O_B$
A atop B	$A \cap B$	$A \cap B \cap \bar{O}_A$	B	O_B
A ratop B	$A \cap B \cap \bar{O}_B$	$A \cap B$	A	O_A
A xor B	$A \cap (\bar{O}_B \cup \bar{O}_A)$	$B \cap (\bar{O}_B \cup \bar{O}_A)$	$(A \cup B) \cap (\bar{O}_A \cup \bar{O}_B)$	$(\bar{B} \cap O_A) \cup (\bar{A} \cap O_B)$

Table 6